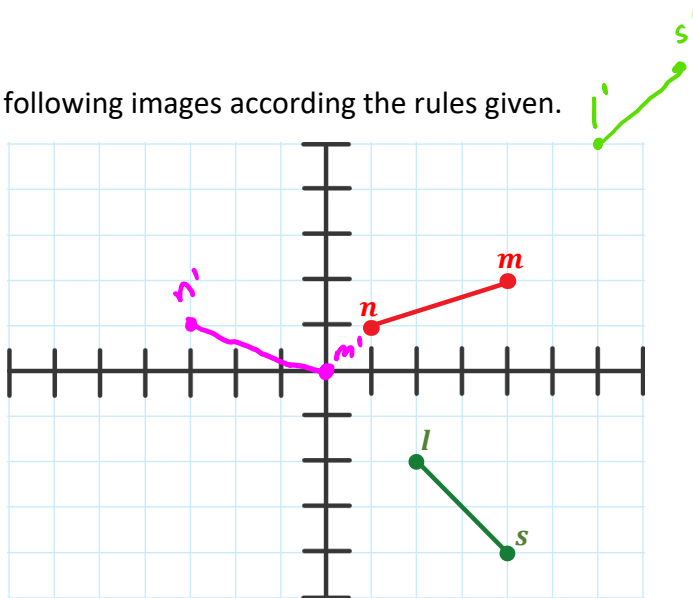


## WARM UP

Translate, **Rotate**, and/or Reflect the following images according the rules given.

$$R_{x\text{-axis}} \circ T_{(-4,-2)}(\overline{MN})$$

$$T_{(4,3)} \circ r_{(90^\circ,0)}(\overline{SL})$$



# ESSENTIAL QUESTION

How can rigid motions be classified?

**NEEDED VOCAB:**

► **Glide Reflection**

**GOAL: "I CAN. . .**

**Identify different rigid motions used to transform two-dimensional shapes."**

Two students are trying to determine whether compositions of rigid motions are commutative. View all of their work in the gallery of images.

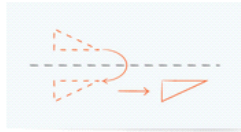
- A. Should Paula have used graph paper? Explain.
- B. Do you agree with Paula or Keenan? Explain.

**Paula's Conclusion**

Translate. Then reflect.



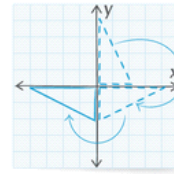
Reflect. Then translate.



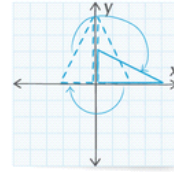
Conclusion: Compositions of rigid motions are commutative.

**Keenan's Conclusion**

Rotate. Then reflect.



Reflect. Then rotate.

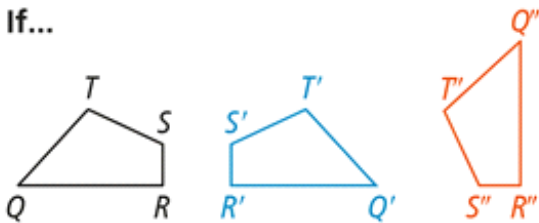


Conclusion: Compositions of rigid motions are **not** commutative.

### Rigid Motion Composition

The composition of two or more rigid motions is a rigid motion.

If...



$M: QRST \rightarrow Q'R'S'T'$  and  
 $N: Q'R'S'T' \rightarrow Q''R''S''T''$  are rigid motions.

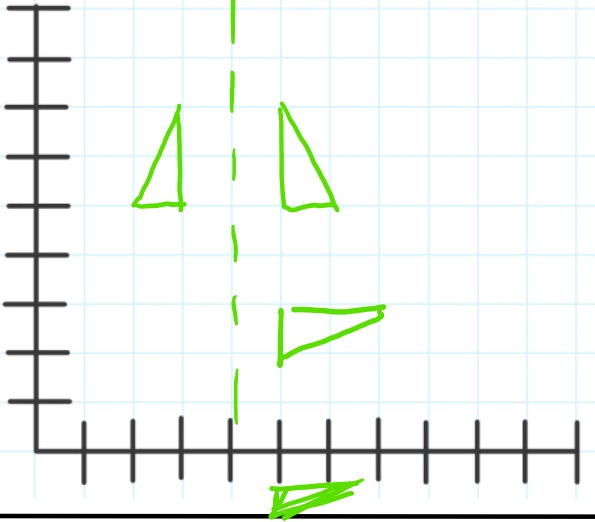
Then...

$(N \circ M): QRST \rightarrow Q''R''S''T''$   
 is a rigid motion.

PROOF: SEE EXAMPLE 1.

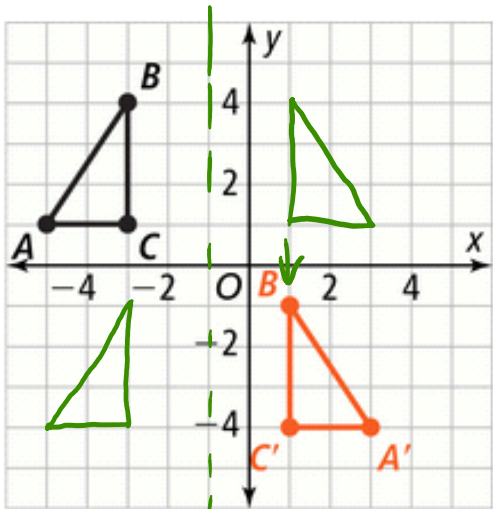
How can we **prove** that a composition of rigid motions is a rigid motion?

Use the Diagram for visual purposes.



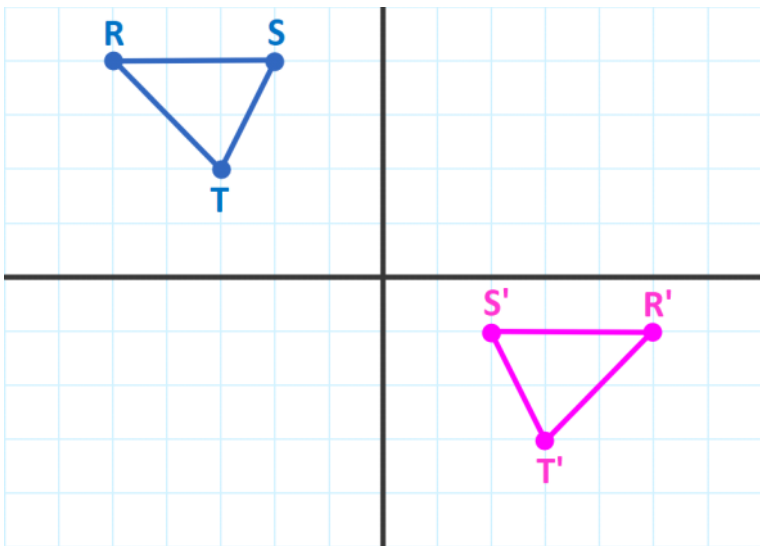
### EXAMPLE 1

Is there a rigid motion that maps  $\triangle ABC$  to  $\triangle A'B'C'$ ?



$$R_{(x=-1)} \circ T_{\langle \emptyset, -5 \rangle}$$

What is the glide reflection that maps  $\triangle RST$  to  $\triangle R'S'T'$ ?



$$R_{(y\text{-axis})} \circ T_{\langle \emptyset, -5 \rangle}$$

Glide Reflection

$$T_{\langle \quad \rangle} \circ R_{(\quad)}$$

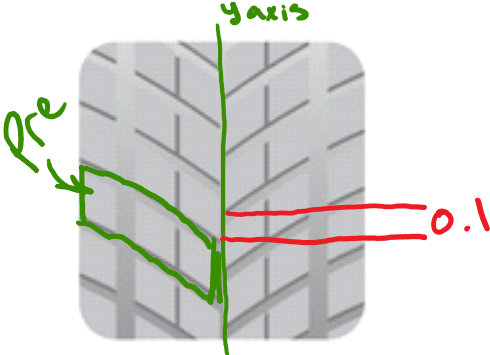
$$R_{(\quad)} \circ T_{\langle \quad \rangle}$$

Reflection is H. or V.  
The translation is the other.

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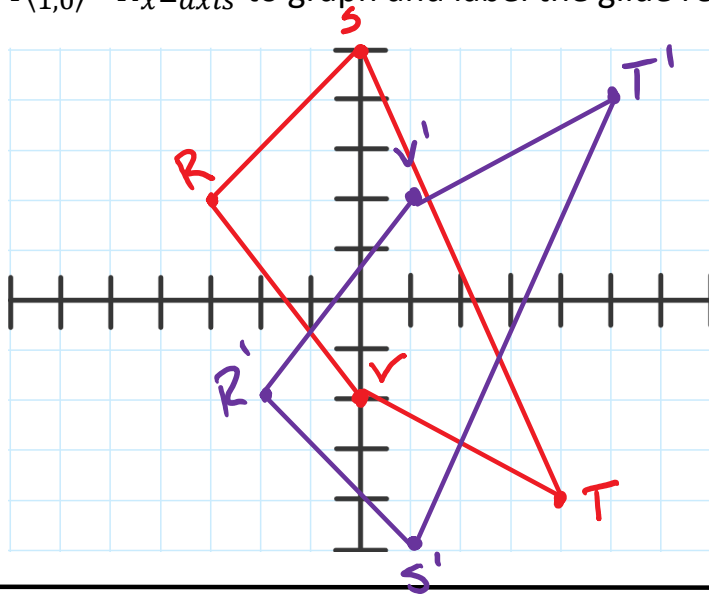
## EXAMPLE 2

A digital artist is reproducing a tire tread pattern from a partial tire print from a crime scene by applying a glide reflection. She uses the rule  $T_{\langle 0,0.1 \rangle} \circ R_{y\text{-axis}}$  to generate a pattern. Confirm that her rule can be applied to the partial pattern that was taken from the crime scene.



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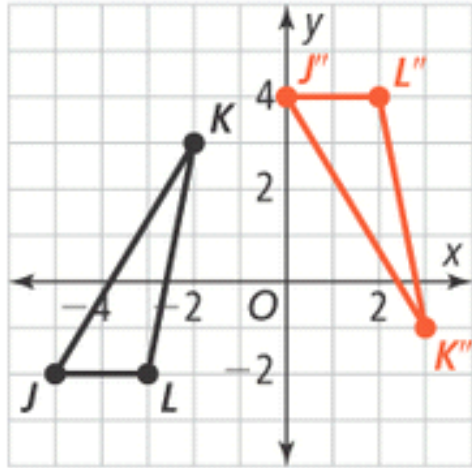
Quadrilateral RSTV has vertices  $R(-3, 2)$ ,  $S(0, 5)$ ,  $T(4, -4)$ ,  $V(0, -2)$ . Use the rule  $T_{\langle 1,0 \rangle} \circ R_{x\text{-axis}}$  to graph and label the glide reflection of RSTV.



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What is the glide reflection that maps  $\triangle JKL$  to  $\triangle J''K''L''$ ?

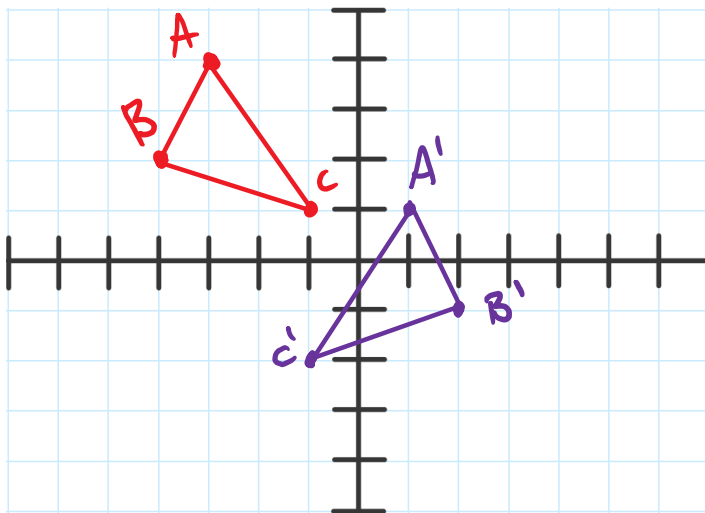
$$T_{\langle 5, 0 \rangle} \circ R_{(y=1)}$$



What is the glide reflection that maps the following?

$\triangle ABC \rightarrow \triangle A'B'C'$  given:

$A(-3, 4)$ ,  $B(-4, 2)$ ,  $C(-1, 1)$ ,  $A'(1, 1)$ ,  $B'(2, -1)$ , and  $C'(-1, -2)$ .



$$T_{\langle 0, -3 \rangle} \circ R_{(x=-1)}$$

What is the glide reflection that maps the following?

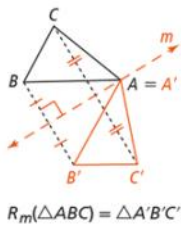
$\overline{RS} \rightarrow \overline{R'S'}$  given:

$R(-2, 4)$ ,  $S(2, 6)$ ,  $R'(4, 0)$ , and  $S'(8, -2)$ .

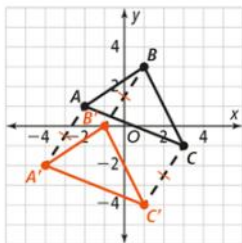
$$T_{\langle 6, 0 \rangle} \circ R_{y=2}$$

Types of Rigid Motions

REFLECTION

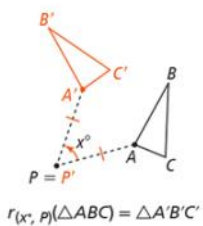


TRANSLATION



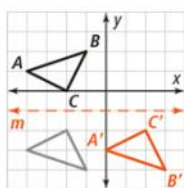
$$T_{(-2, -3)}(\Delta ABC) = \Delta A'B'C'$$

ROTATION



$$r_{(x^\circ, P)}(\Delta ABC) = \Delta A'B'C'$$

GLIDE REFLECTION



$$(T_{(4, 0)} \circ R_m)(\Delta ABC) = \Delta A'B'C'$$

# HOMework

Pg. 134

9, 10, 12-21, 25, 26