## Warm Up

Find the missing measure to make the objects similar.


## Essential Question

How can you use the angles and sides of two triangles to determine whether they are similar?

GOAL: "I CAN...
Use dilation and rigid motion to establish triangle similarity theorems."


Would any triangle with two angles measuring $40^{\circ}$ and $60^{\circ}$ be similar to $\triangle A B C$ ?

## EXAMPLE 1

If $\angle A \cong \angle R$ and $\angle B \cong \angle S$, is $\triangle A B C \sim \triangle R S T$ ? Explain.


1. If $\angle A$ is congruent to $\angle R$, and $\angle C$ is congruent to $\angle T$, how would you prove the triangles are similar?

2. It $\angle A$ is congruent to $\angle \kappa$, and $\angle C$ is congruent to $\angle T$, how would you prove the triangles are similar?


## Angle-Angle Similarity (AA ~) Theorem

> If two angles of one triangle are congruent to two angles of another triangle, then the triangles are similar.

PROOF: SEE EXERCISE 10.


$$
\angle A \cong \angle D \text { and } \angle B \cong \angle E
$$

Then... $\triangle A B C \sim \triangle D E F$

If $\frac{L M}{P Q}=\frac{M N}{Q R}=\frac{L N}{P R}$, is there a similarity transformation that maps $\triangle P Q R$ to $\triangle L M N$ ? Explain.

2. If $\frac{D F}{G J}=\frac{E F}{H J}$ and $\angle F \cong \angle J$, is there a similarity transformation that maps $\triangle D E F$ to $\triangle G H J$ ? Explain.


## Side-Side-Side Similarity (SSS ~) Theorem

If the corresponding sides of two triangles are proportional, then the triangles are similar.

If...


$$
\frac{A B}{D E}=\frac{B C}{E F}=\frac{A C}{D F}
$$

Then... $\triangle A B C \sim \triangle D E F$

## Side-Angle-Side Similarity (SAS ~) Theorem

If an angle of one triangle is congruent to an angle of a second triangle, and the sides that include the two angles are proportional, then the triangles are similar.

PROOF: SEE EXERCISE 13.

If...


$$
\angle B \cong \angle E \text { and } \frac{A B}{D E}=\frac{B C}{E F}
$$

Then... $\triangle A B C \sim \triangle D E F$

## A. Are $\triangle A B C$ and $\triangle D E F$ similar?



## B. Are $\triangle P Q S$ and $\triangle R Q P$ similar?


3. a. Is $\triangle A D E \sim \triangle A B D$ ? Explain.

b. Is $\triangle A D E \sim \triangle B D C$ ? Explain.

## What is MN?


4. a. If the measure of $\overline{J L}$ were 150 instead of 75 , how would the value of $M N$ be different?
b. If the measure of $\overline{J K}$ were 20 instead of 10, how would the
 value of $M N$ be different?

## Avery puts up a radio antenna

 tower in his yard. Ella tells him that their city has a law limiting towers to 50 ft in height. How can Avery use the lengths of his shadow and the shadow of the tower to show that his tower is within the limit without directly measuring it?
5. If the tower were 50 ft tall, how long would the shadow of the tower be?



## Homework

Pg. 322<br>10, 11, 16-20, 22, 26

