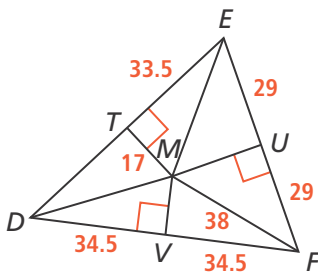


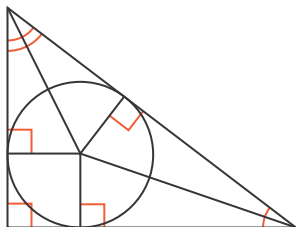
**UNDERSTAND**

- Construct Arguments** Write a Proof of Theorem 5-6: In  $\triangle ABC$ , let the angle bisectors of  $\angle A$  and  $\angle B$  intersect at point  $P$ . Show that  $P$  is equidistant from each side of  $\triangle ABC$ , and that  $\overline{CP}$  bisects  $\angle C$ .
- Higher Order Thinking** A right triangle has vertices  $X(0, 0)$ ,  $Y(0, 2a)$ ,  $Z(2b, 0)$ . What is the circumcenter of the triangle? Make a conjecture about the diameter of a circle that is circumscribed about a right triangle.
- Error Analysis** What is the error that a student made in finding the perimeter of  $\triangle DTM$ ? Correct the error.



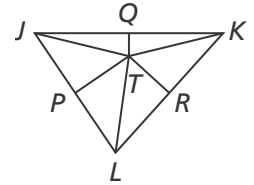
$DT = 34.5, TM = 17, DM = 34.5$ .  
The perimeter of  $\triangle DTM$  is  
 $34.5 + 17 + 34.5 = 86$ . **X**

- Mathematical Connections** A triangle with incenter  $P$  has side lengths  $x, y$ , and  $z$ . The distance from  $P$  to each side is  $a$ . Write an expression for the area of the triangle. Use the distributive property to factor your expression.
- Reason** In a right triangle with side lengths of 3, 4, and 5, what is the radius of the inscribed circle? Show your work. (Hint: Let  $r$  be the radius. Label the lengths of each segment formed by the perpendiculars to the sides.)

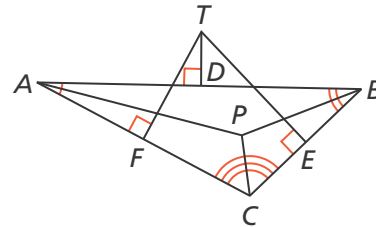


**PRACTICE**

- The perpendicular bisectors of  $\triangle JKL$  are  $\overline{PT}$ ,  $\overline{QT}$ , and  $\overline{RT}$ . Name three isosceles triangles. SEE EXAMPLE 1

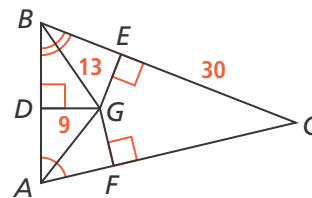


Use the diagram below for Exercises 16-18. Points  $D, E$ , and  $F$  are the midpoints of the sides of  $\triangle ABC$ . SEE EXAMPLES 2 AND 4



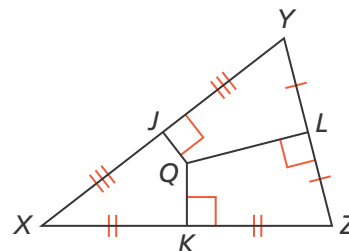
- Which point is the center of a circle that contains  $A, B$ , and  $C$ ?
- Which point is the center of a circle that intersects each side of  $\triangle ABC$  at exactly one point?
- The perpendicular bisector of  $\overline{AB}$  is  $m$  and the perpendicular bisector of  $\overline{BC}$  is  $n$ . Lines  $m$  and  $n$  intersect at  $T$ . If  $TA = 8.2$ , what is  $TC$ ?  
SEE EXAMPLE 3

**Find the values.** SEE EXAMPLE 5



- $EG$
- $GF$

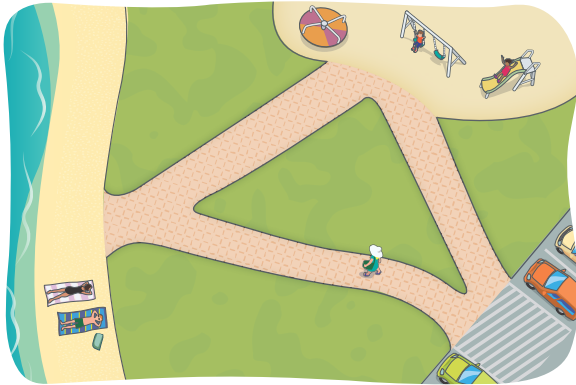
If  $XY = 24$ ,  $XZ = 22$ , and  $JQ = 5$ , find the values. Round to the nearest tenth.



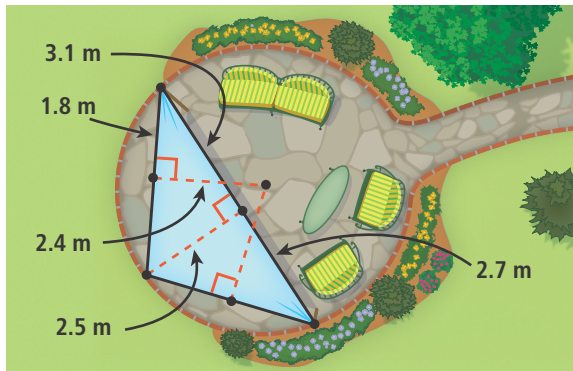
- The radius of the circumscribed circle of  $\triangle XYZ$
- $QK$

**APPLY**

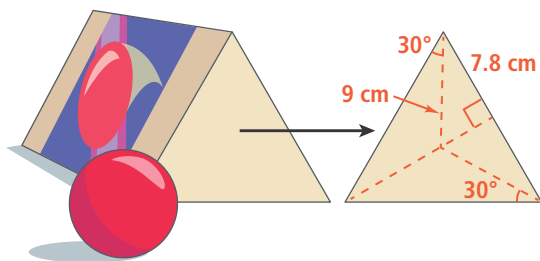
**23. Model With Mathematics** A maintenance crew wants to build a shed at a location that is the same distance from each path. Where should the shed be located? Justify your answer with a diagram.



**24. Reason** What is the area of the patio **not** covered by the sunshade? Round to the nearest tenth, and explain how you found your answer.



**25. Make Sense and Persevere** A ball manufacturer wants to stack three balls, each with an 8-centimeter diameter, in a box that is an equilateral triangular prism. The diagram shows the dimensions of the bases. Will the balls fit in the box? Explain how you know.



**ASSESSMENT PRACTICE**

**26.** In  $\triangle ABC$ ,  $\overline{AB}$  has midpoint  $M$ , and  $\ell$  is the perpendicular bisector of  $\overline{AB}$  and the angle bisector of  $\angle ACB$ . Which of the following must be true? Select all that apply.

- (A) The radius of the inscribed circle of  $\triangle ABC$  is  $AM$ .
- (B)  $AC = CB$
- (C) Both the circumcenter and incenter of  $\triangle ABC$  are on  $\ell$ .
- (D) The circumcenter of  $\triangle ABC$  is inside the triangle.

**27. SAT/ACT** Circle  $O$  intersects  $\overline{AB}$  only at  $F$ ,  $\overline{BC}$  only at  $G$ , and  $\overline{AC}$  only at  $H$ . Which equation is true?

- (A)  $AH = AC$
- (B)  $m\angle OFB = 90$
- (C)  $OB = OC$
- (D)  $OF = OC$
- (E)  $\angle BAO \cong \angle ABO$

**28. Performance Task** Edison High School is designing a new triangular pennant. The school mascot will be inside a circle, and the circle must touch each side of the pennant. The circle should fill as much of the pennant as possible.



**Part A** Using a straightedge and compass, draw at least 4 different types of triangles for the pennant. Construct an inscribed circle in each triangle.

**Part B** Make a table about your pennants. Include side lengths, type of triangle, circle radius and area, triangle area, and ratio of circle area to triangle area.

**Part C** What type of triangle do you recommend that they use? Justify your answer.