## UNDERSTAND

12. Error Analysis What is Benson's error?


$$
\begin{aligned}
\frac{5}{10} & =\frac{x}{7} \\
10 x & =35 \\
x & =3.5
\end{aligned}
$$

13. Mathematical Connections What percent of the area of $\triangle P Q R$ is the area of $\triangle Q R S$ ? Explain.

14. Construct Arguments Write a proof of the Side-Splitter Theorem.
Given: $\overline{M N} \| \overline{A C}$
Prove: $\frac{A M}{M B}=\frac{C N}{N B}$

15. Higher Order Thinking Suppose $O, P$, and $Q$ are midpoints of the sides of $\triangle L M N$. Show that $\triangle L O Q$, $\triangle O M P, \triangle Q P N$, and $\triangle P Q O$ are congruent to each other.

16. Construct Arguments Write a proof for the Triangle-AngleBisector Theorem.
Given: $\overrightarrow{A D}$ bisects $\angle A$.
Prove: $\frac{C A}{A B}=\frac{C D}{D B}$
Use the following outline.


- Extend $\overrightarrow{C A}$ and draw a line through point $B$ parallel to $\overrightarrow{A D}$ that intersects $\overrightarrow{C A}$ at point $E$.
- Show that $\frac{C A}{A E}=\frac{C D}{D B}$.
- Then show that $\triangle A E B$ is isosceles.



## PRACTICE

For Exercises 17-19, find each value.
SEE EXAMPLES 1 AND 2

17. $x$
18. $y$
19. $z$
20. What is the value of $x$ ? SEE EXAMPLE 3


For Exercises 21-23, find each value of $x$ for the given value of $y$. Round to the nearest tenth.
SEE EXAMPLES 4 AND 5

21. $y=16$
22. $y=20$
23. $y=18$
24. Write a proof of the Triangle Midsegment Theorem.

Given: $\overline{D G} \cong \overline{G E}, \overline{F H} \cong \overline{H E}$
Prove: $\overline{G H} \| \overline{D F}, G H=\frac{1}{2} D F$

25. Write a proof of the Corollary to the Side-Splitter Theorem.

Given: $\ell\|m\| n$
Prove: $\frac{A B}{B C}=\frac{D E}{E F}$
Hint: Draw $\overline{A F}$. Label the intersection of $\overline{A F}$ and $\overleftrightarrow{B E}$ point $G$.


## APPLY

26. Use Structure A building in the shape of a pyramid needs to have supports repaired, and two parallel sections need to be reinforced. The face of the building is an equilateral triangle. What are the lengths of $\overline{K O}$ and $\overline{L N}$ ?

27. Higher Order Thinking Use the figure to prove Theorem 2-13: Two non-vertical lines are parallel if and only if they have the same slope.

a. Assume the slopes of lines $m$ and $n$ are equal. Use proportions in $\triangle A C E$ and $\triangle B C D$ to show that $m \| n$.
b. Now assume that $m \| n$. Show that the slopes of $m$ and $n$ are equal.
28. Use Structure Aisha is building a roof and needs to determine the lengths of $\overline{C G}$ and $\overline{C F}$ from the design shown. How can she determine $C G$ and $C F$ ? What are CG and CF?


## ASSESSMENT PRACTICE

29. What is the value of $x$ ?

30. SAT/ACT What is the measure of side $C B$ ?

(A) 4.57
(B) 6.4
© 8.96
(D) 9.4
31. Performance Task Emma is determining measurements needed to simulate the distances in a shuffleboard computer game that she is programming.


Part A The horizontal lines must be parallel and in proportion so that each zone of the shuffleboard appears to be the same length. What are the lengths $w, x$, and $y$ ?

Part B What is the length of each horizontal segment?

Part C Which horizontal segment is closest to the midsegment of the triangle that extends off of the screen? How do you know?

